

# *King Fahd University of Petroleum & Minerals*

**Department of Civil and Environmental Engineering**

**CE 201 – Statics**

**Semester:** 151  
**Examination:** First Major  
**Date (Day):** October 10, 2015 (Sunday)  
**Time:** 07:00 – 09:00 p.m.

Section	1	2	3	4	5	6	7	8
Instructor	Al-Malack	Al-Malack	Vohra	Al-Osta	Al-Attas	Essa	Al-Amoudi	Chowdhury
Time	07:00	08:00	08:00	09:00	10:00	11:00	13:10	07:00
Tick								

Student's Name :
Student's ID :

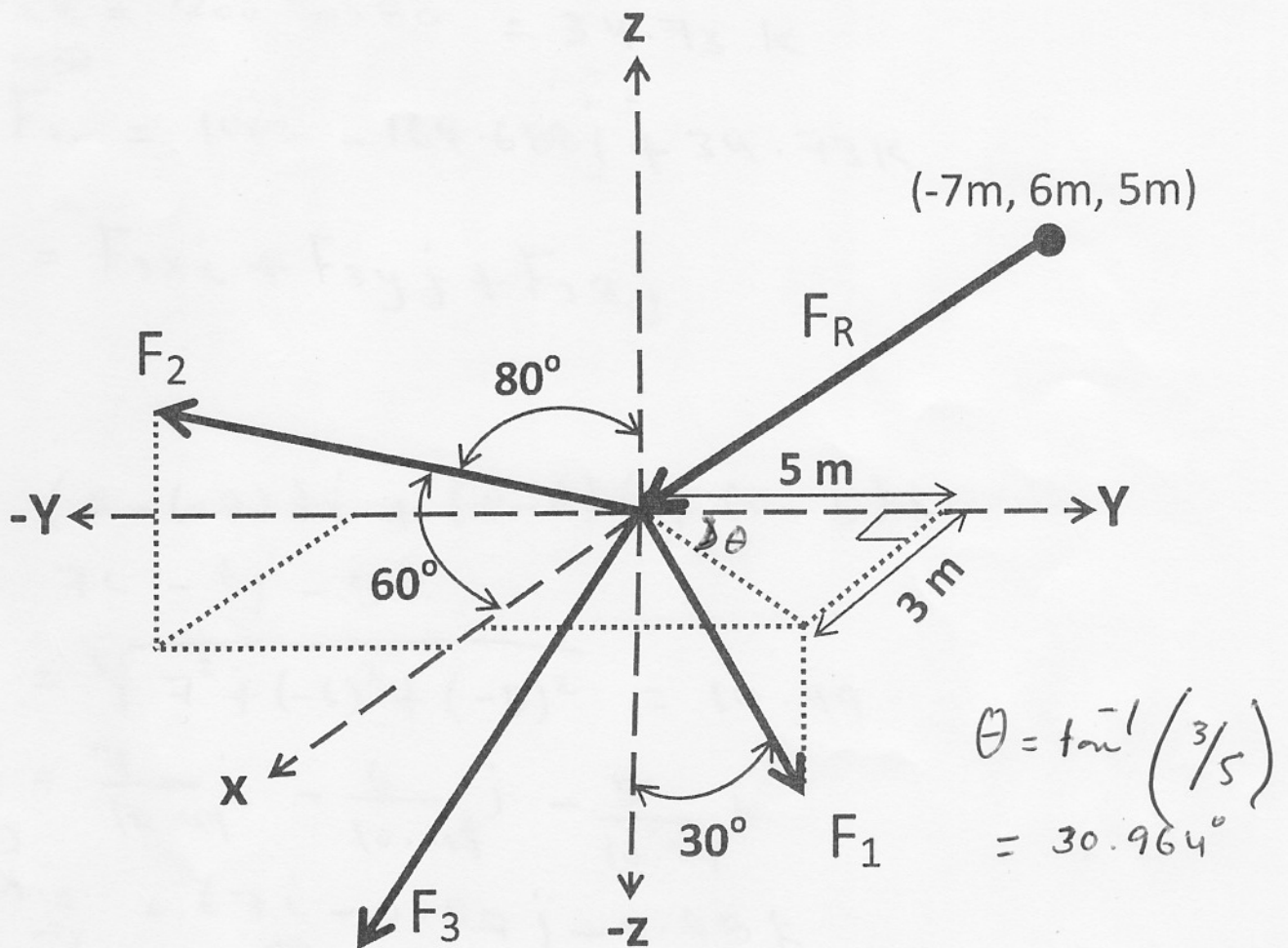
Problem	Assigned Grade	Earned Grade
1	25 (Points)	
2	25 (Points)	
3	25 (Points)	
4	25 (Points)	
<b>Total</b>	<b>100 (Points)</b>	

*Good Luck*

### Problem 1 (25 Points)

Using Cartesian Vector Formulation, Find the magnitude and directional angles of  $F_3$  of the forces shown in the figure if:

- $F_1 = 100$  kN;
- $F_2 = 200$  kN;
- The resultant force  $F_R$  of the  $F_1$ ,  $F_2$  and  $F_3 = 400$  kN



$F_1$ :

$$F_{1z} = -100 \cos 30 = -86.603 \text{ k}$$

$$F_1' = 100 \sin 30 = 50$$

$$F_{1x} = 50 \times \sin 30.964 = 25.725 \text{ i}$$

$$F_{1y} = 50 \times \cos 30.96 = 42.88 \text{ j}$$

$$\vec{F}_1 = 25.725 \text{ i} + 42.875 \text{ j} - 86.603 \text{ k}$$

$F_2$  :-

$$\therefore \cos^2 60 + \cos^2 \beta + \cos^2 80 = 1$$

$$\Rightarrow \beta = 31.96^\circ \quad \text{or} \quad \beta = 148.04^\circ$$

By inspection:  $\beta = 148.04^\circ$

$$\Rightarrow F_{2x} = 200 \cos 60 = 100i$$

$$F_{2y} = 200 \cos 148.04 = -169.688j$$

$$F_{2z} = 200 \cos 80 = 34.73k$$

$\Rightarrow$

$$\Rightarrow F_2 = 100i - 169.688j + 34.73k$$

$\rightarrow$

$$F_3 = F_{3x}i + F_{3y}j + F_{3z}k$$

$F_R$ :

$$\vec{r} = (0 - (-7))i + (0 - 6)j + (0 - 5)k$$

$$r = 7i - 6j - 5k$$

$$|r| = \sqrt{7^2 + (-6)^2 + (-5)^2} = 10.49$$

$$\Rightarrow \vec{u} = \frac{7}{10.49}i - \frac{6}{10.49}j - \frac{5}{10.49}k$$

$$\vec{u} = 0.67i - 0.57j - 0.48k$$

$$\Rightarrow F_R = 400\vec{u} = 266.97i - 228.83j - 190.69k$$

$$\therefore \sum F = F_R = \vec{F}_1 + \vec{F}_2 + \vec{F}_3$$

$$266.97i - 228.83j - 190.69k = (25.725 + 100 + F_{3x})i + (42.875 + 169.688 + F_{3y})j + (-86.603 + 34.73 + F_{3z})k$$

$$\Rightarrow F_{3x} = 141.245 \text{ KN}$$

$$F_{3y} = -102.02 \text{ KN}$$

$$F_{3z} = -138.82 \text{ KN}$$

Magnitude of  $F_3$

$$\Rightarrow |F_3| = \sqrt{141.245^2 + (-102.02)^2 + (-138.82)^2} = 222.77 \text{ KN}$$

Directional angles of  $F_3$

$$\Rightarrow \alpha = \cos^{-1} \left( \frac{141.245}{222.77} \right) = 50.65^\circ$$

$$\beta = \cos^{-1} \left( \frac{-102.02}{222.77} \right) = 112.25^\circ$$

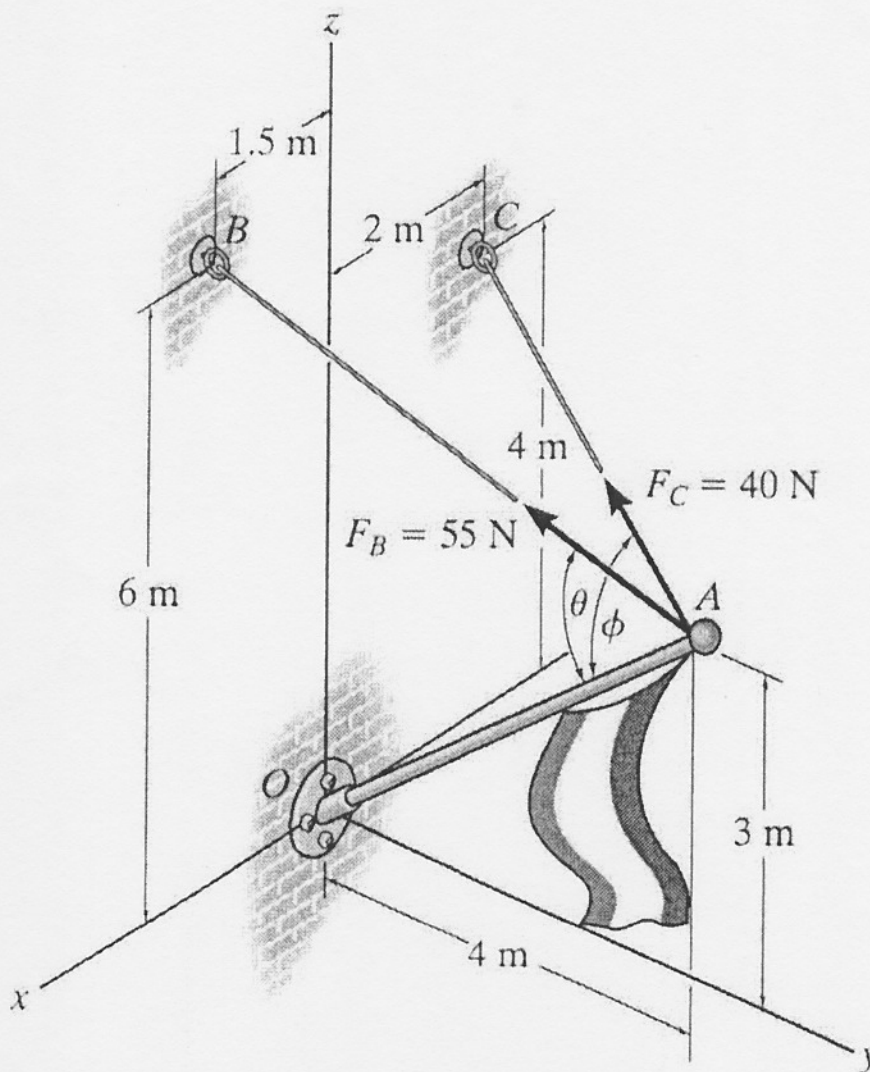
$$\gamma = \cos^{-1} \left( \frac{-138.82}{222.77} \right) = 128.55^\circ$$

### Problem 2 (25 Points)

For the figure shown below:

Use the **DOT PRODUCT** to determine the angles  $\theta$  between the axes OA of the flag pole and cable AB.

Use the **DOT PRODUCT** to determine the projection of force  $F_B$  along cable AC



**Answer:**

**3** Coordinates of points A, B and C are:

$$O = (0, 0, 0) \text{ m}$$

$$A = (0, 4, 3) \text{ m}$$

$$B = (1.5, 0, 6) \text{ m}$$

$$C = (-2, 0, 4) \text{ m}$$

**4** The force exerted by cables AB:

$$\mathbf{F}_B = F_B \mathbf{u}_{AB}$$

$$\mathbf{u}_{AB} = \frac{\mathbf{r}_{AB}}{r_{AB}}$$

$$\mathbf{r}_{AB} = (1.5 - 0) \mathbf{i} + (0 - 4) \mathbf{j} + (6 - 3) \mathbf{k} = [1.5 \mathbf{i} - 4 \mathbf{j} + 3 \mathbf{k}] \text{ m}$$

$$r_{AB} = \sqrt{1.5^2 + 4^2 + 3^2} = 5.22 \text{ m}$$

$$\mathbf{u}_{AB} = \frac{1.5}{5.22} \mathbf{i} - \frac{4}{5.22} \mathbf{j} + \frac{3}{5.22} \mathbf{k}$$

$$\mathbf{F}_B = 55 \left( \frac{1.5}{5.22} \mathbf{i} - \frac{4}{5.22} \mathbf{j} + \frac{3}{5.22} \mathbf{k} \right) = [15.80 \mathbf{i} - 42.15 \mathbf{j} + 31.61 \mathbf{k}] \text{ N}$$

**4** The force exerted by cables AC:

$$\mathbf{F}_C = F_C \mathbf{u}_{AC}$$

$$\mathbf{u}_{AC} = \frac{\mathbf{r}_{AC}}{r_{AC}}$$

$$\mathbf{r}_{AC} = (-2 - 0) \mathbf{i} + (0 - 4) \mathbf{j} + (4 - 3) \mathbf{k} = [-2 \mathbf{i} - 4 \mathbf{j} + 1 \mathbf{k}] \text{ m}$$

$$r_{AC} = \sqrt{2^2 + 4^2 + 1^2} = 4.58 \text{ m}$$

$$\mathbf{u}_{AC} = -\frac{2}{4.58} \mathbf{i} - \frac{4}{4.58} \mathbf{j} + \frac{1}{4.58} \mathbf{k}$$

$$\mathbf{F}_{AC} = 40 \left( -\frac{2}{4.58} \mathbf{i} - \frac{4}{4.58} \mathbf{j} + \frac{1}{4.58} \mathbf{k} \right) = [-17.47 \mathbf{i} - 34.93 \mathbf{j} + 8.73 \mathbf{k}] \text{ N}$$

4 The position vector of the flag pole:

$$\mathbf{r}_{AO} = (0 - 0)i + (0 - 4)j + (0 - 3)k = [0i - 4j - 3k] \text{ m}$$

$$r_{AO} = \sqrt{0^2 + 4^2 + 3^2} = 5 \text{ m}$$

1. The angle  $\theta$  between the forces exerted by cables AB and AC using **DOT PRODUCT**.

3  $\mathbf{F}_B \cdot \mathbf{r}_{AO} = F_B r_{AO} \cos \theta$

$$(15.80i - 42.15j + 31.61k) \cdot (0i - 4j - 3k) = (55)(5) \cos \theta$$

$$[(15.80)(0)] + [(-42.15)(-4)] + [(31.61)(-3)] = (55)(5) \cos \theta$$

2  $\theta = \cos^{-1} \left( \frac{73.77}{275} \right) = 74.44^\circ$

2. The magnitude of the projection of  $\mathbf{F}_B$  along the cable AC using the **DOT PRODUCT**.

3 Projection of  $\mathbf{F}_B$  along the cable AC =  $\mathbf{F}_B \cdot \mathbf{u}_{AC}$

$$= 55 \left( \frac{1.5}{5.22}i - \frac{4}{5.22}j + \frac{3}{5.22}k \right) \cdot \left( -\frac{2}{4.58}i - \frac{4}{4.58}j + \frac{1}{4.58}k \right)$$

$$= [(15.80)(-0.44)] + [(-42.15)(-0.87)] + [(31.61)(0.22)]$$

2 = 36.67 N

**Problem 3 (25 Points)**

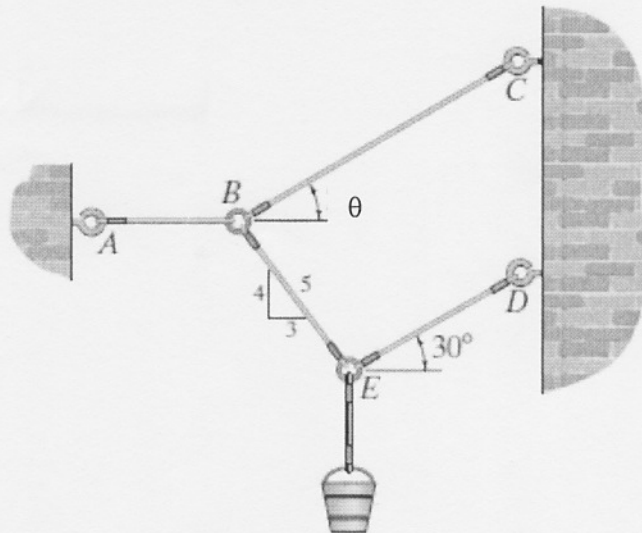
In the figure shown below, If tensions in Cables BC and BE are:

$$T_{BC} = 0.35 \text{ kN}$$

$$T_{BE} = 0.22 \text{ kN}$$

**Find:**

- A.  $T_{AB}$
- B.  $T_{ED}$
- C. Weight of the bucket
- D. Angle  $\theta$

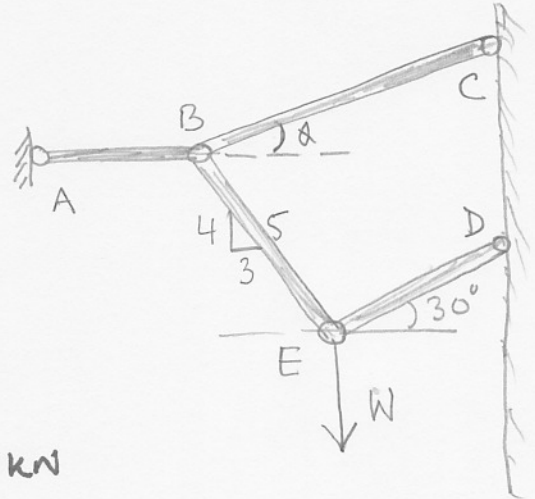




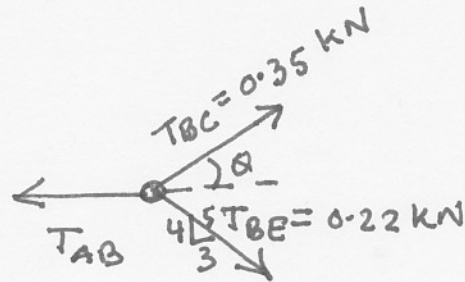
Q.3

The tensions in cables BC and BE are 0.35 kN and 0.22 kN respectively.

Solution:



Joint B

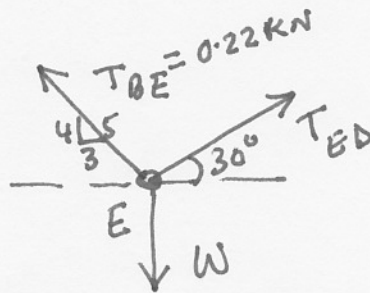


$$\Sigma F_x = 0 = -T_{AB} + 0.35 \cos \alpha + \frac{3}{5} \times 0.22$$

$$\Sigma F_y = 0 = 0.35 \sin \alpha - \frac{4}{5} \times 0.22 \Rightarrow \boxed{\alpha = 30.2^\circ}$$

$$\therefore \boxed{T_{AB} = 0.434 \text{ kN}}$$

Joint E:



$$\Sigma F_x = 0 \Rightarrow \frac{3}{5} \times 0.22 + T_{ED} \cos 30^\circ \Rightarrow \boxed{T_{ED} = 0.152 \text{ kN}}$$

$$\Sigma F_y = 0 = T_{ED} \sin 30^\circ - W + T_{BE} \times \frac{4}{5}$$

$$\Rightarrow W = 0.252 \text{ kN}$$

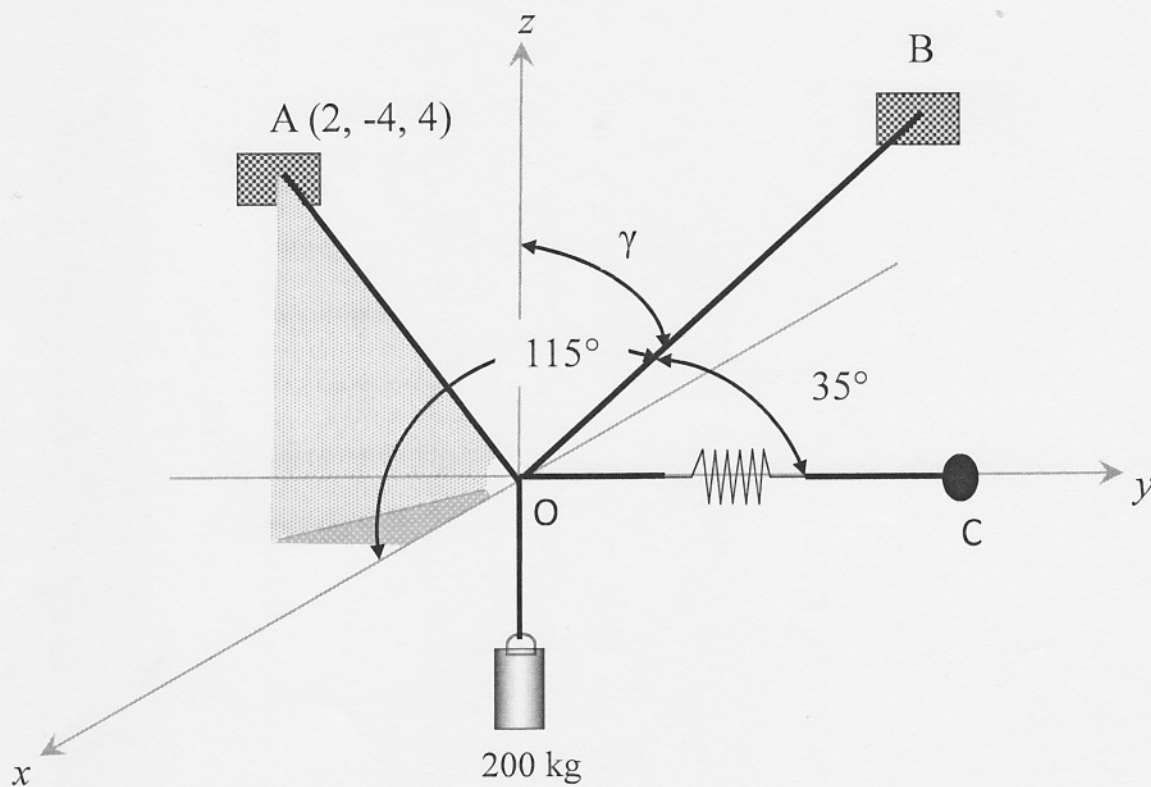
$$\therefore m = \frac{252}{9.81} = 25.7$$

$$\therefore \boxed{m = 26 \text{ kg}}$$

**Problem 4 (25 Points)**

The system shown below is supporting a mass of 200 kg. The spring OC has stiffness  $k$  value of 0.7 kN/m. Determine:

- Tensions in cables OA and OB.
- Stretch of spring OC.



Q 4

$$\rightarrow W = mg = 1962 \text{ N}$$

$$\vec{W} = \{-1962 \text{ k}\} \text{ N}$$

$$\rightarrow \vec{F}_{OC} = \{F_{OC} \text{ j}\} \text{ N} = \{700 \text{ s i j}\} \text{ N}$$

$$\rightarrow \vec{F}_{OB} = F_{OB} \cos \alpha \text{ i} + F_{OB} \cos \beta \text{ j} + F_{OB} \cos \nu \text{ k}$$

$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \nu = 1$$

$$\nu = \pm 0.387$$

$$= 67.2^\circ \text{ or } 112.76^\circ$$

$$\text{By inspection } \nu = 67.2^\circ$$

$$\therefore \vec{F}_{OB} = -0.423 F_{OB} \text{ i} + 0.819 F_{OB} \text{ j} + 0.388 F_{OB} \text{ k}$$

$$\rightarrow \vec{F}_{OA} = F_{OA} \vec{U}_{OA} = F_{OA} \frac{\vec{r}_{OA}}{r_{OA}}$$

$$\vec{r}_{OA} = 2\text{i} - 4\text{j} + 4\text{k}$$

$$r_{OA} = \sqrt{2^2 + (-4)^2 + (4)^2} = 6 \text{ m}$$

$$\therefore \vec{F}_{OA} = 0.333 F_{OA} \text{ i} - 0.667 F_{OA} \text{ j} + 0.667 F_{OA} \text{ k}$$

$$\rightarrow \sum F_x = -0.423 F_{OB} + 0.333 F_{OA} = 0$$

$$\sum F_y = F_{OC} + 0.819 F_{OB} - 0.667 F_{OA} = 0$$

$$\sum F_z = 0.388 F_{OB} + 0.667 F_{OA} - 1962 = 0$$

Solving gives

$$F_{OC} = 44.902 \text{ N}$$

$$F_{OB} = 1588.3 \text{ N}$$

$$F_{OA} = 2017.6 \text{ N}$$

$$\rightarrow s = \frac{F_{OC}}{700} = 0.064 \text{ m}$$