

```
syms Vs Vr delta R X real
syms Is
```

Current is specified as:

```
Is=simplifyFraction((Vs*(cos(delta)+1i*sin(delta))-Vr)/(R+1i*X))
```

$$I_s = \frac{V_s \cos(\delta) - V_r + V_s \sin(\delta) i}{R + X i}$$

Complex power is: $V_s \cdot \text{conj}(I_s)$

```
S=simplify(Vs*(cos(delta)+1i*sin(delta))*conj(Is))
```

$$S = - \frac{V_s (\cos(\delta) + \sin(\delta) i) (V_r - V_s \cos(\delta) + V_s \sin(\delta) i)}{R - X i}$$

Real power is: $\text{Re}(\text{complex power})$

```
P=simplify(real(S))
```

$$P = \frac{V_s (R V_s - R V_r \cos(\delta) + V_r X \sin(\delta))}{R^2 + X^2}$$

Reactive power is: $\text{imag}(\text{complex power})$

```
Q=simplify(imag(S))
```

$$Q = - \frac{V_s (V_r X \cos(\delta) - V_s X + R V_r \sin(\delta))}{R^2 + X^2}$$

Real power equation with resistance neglected:

```
P=simplify(real(subs(S,R,0)))
```

$$P = \frac{V_r V_s \sin(\delta)}{X}$$

Reactive power with resistance neglected:

```
Q=simplify(imag(subs(S,R,0)))
```

$$Q = \frac{V_s (V_s - V_r \cos(\delta))}{X}$$

Calculating values of real and reactive power with the line resistance included:

R=5.1842 Ohms X=129.605 Ohms Vs = Vr = 161kV delta = 0.01877218

```
Q=double(imag(subs(S,[Vs,Vr,R,X,delta],[161e3,161e3,5.1842,1.29605e2,0.01877218])))
```

Q =
-1.147465859708760e+05

```
P=double(real(subs(S,[Vs,Vr,R,X,delta],[161e3,161e3,5.1842,1.29605e2,0.01877218])))
```

P =
3.749625633195513e+06

Calculating values of real and reactive power with the line resistance neglected

R=0 Ohms X=129.605 Ohms Vs = Vr = 161kV delta = 0.01877218

```
Q=double(imag(subs(S,[Vs,Vr,R,X,delta],[161e3,161e3,0,1.29605e2,0.01877218])))
```

Q =
3.523843935694449e+04

```
P=double(real(subs(S,[Vs,Vr,R,X,delta],[161e3,161e3,0,1.29605e2,0.01877218])))
```

P =
3.754215496634348e+06

As can be seen the values of P for both cases are very close (approx 3.75MW). Bu the values for Q are very different.