## Problem A. Hill

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 2 seconds |
| Memory limit: | 256 megabytes |

Amanbol has a table $A$ of size $n \times m$. The rows of the table are numbered from 1 to $n$, and the columns are numbered from 1 to $m$. Each cell of the table either contains the character ' X ', or one digit from ' 0 ' to ' 9 '.
If the symbol ' X ' is written on a table cell, it means that Amanbol marked this cell as blocked. Otherwise, the number written on this cell denotes its value.
After a recent hike in the mountains, Amanbol wants to find a hill in his table. He defines a hill as follows:

1. First we choose two numbers $(s, e)$ such that $(1 \leq s \leq e \leq n)$.
2. Then for each $k(s \leq k \leq e)$ we choose a pair $\left(L_{k}, R_{k}\right)$ such that $\left(1 \leq L_{k} \leq R_{k} \leq m\right)$.
3. The conditions $L_{s} \geq L_{s+1} \geq \ldots \geq L_{e}$ and $R_{s} \leq R_{s+1} \leq \ldots \leq R_{e}$ should be satisfied.

Let's say that a cell $(x, y)$ belongs to a hill if $s \leq x \leq e$ and $L_{x} \leq y \leq R_{x}$. Among all possible hills, Amanbol wants to find the one with no blocked cells and the total value of all its cells is maximum. Help him with this task!

## Input

The first line of the input contains two integers $n$ and $m(1 \leq n, m \leq 2500)$ - the number of rows and columns in table $A$.
The $i$-th of the next $n$ lines contains exactly $m$ characters $A_{i, 1}, \ldots, A_{i, m}$.
It is guaranteed that each table cell is a character ' $x$ ' or a digit from ' 0 ' to ' 9 '. It is also guaranteed that it is always possible to find at least one hill in the table.

## Output

Print a single integer - the maximum possible total value of all cells of the hill.

## Scoring

This task contains 5 subtasks.

| Subtask | Additional restrictions | Points | Required subtasks |
| :---: | :---: | :---: | :---: |
| 0 | Examples | 0 | - |
| 1 | $n=1$ | 12 | - |
| 2 | No blocked cells | 7 | - |
| 3 | $n, m \leq 50$ | 25 | 0 |
| 4 | $n, m \leq 300$ | 22 | 3 |
| 5 | - | 34 | $1,2,4$ |

## Examples

|  | standard input |
| :--- | :--- |
| 44 | 19 |
| 5175 | standard output |
| 312 X |  |
| 1XX9 |  |
| 16 X8 |  |
| 1 123X4 | 5 |

## Note



First example

In the first example, for instance, the following hills are possible:

1. Let's choose $s=3, e=4$. Then choose $\left(L_{3}, R_{3}\right)=(4,4)$ and $\left(L_{4}, R_{4}\right)=(4,4)$ (marked in red in the first image). The total value of the cells of this hill is $9+8=17$.
2. Let's choose $s=1, e=4$. Then choose $\left(L_{k}, R_{k}\right)=(1,1)$ for all $k(1 \leq k \leq 4)$ (marked in green in the first image). The total value of the cells of this hill is $5+3+1+2=11$.
3. Let's choose $s=1, e=2$. Then choose $\left(L_{1}, R_{1}\right)=(1,3)$ and $\left(L_{2}, R_{2}\right)=(1,3)$ (marked in blue in the first image). The total value of the cells of this hill is 19 .

And the following hills, for example, are invalid:

1. Let's choose $s=1, e=2$. Then choose $\left(L_{1}, R_{1}\right)=(1,4)$ and $\left(L_{2}, R_{2}\right)=(1,3)$ (marked in green in the second image). This hill is invalid because the condition $R_{1} \leq R_{2}$ is not fulfilled.
2. Let's choose $s=4, e=4$. Then choose $\left(L_{4}, R_{4}\right)=(1,4)$ (marked in red in the second image). This hill is invalid because the hill contains a blocked cell $(4,3)$.

It can be shown that among all possible hills, the maximum total value of cells will be equal to 19 .

## Problem B. Two tree

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 4 seconds |
| Memory limit: | 512 megabytes |

Temirlan, as a true friend, gave Dimash two trees. These trees, however, were not the usual trees you might encounter but two undirected connected graphs without cycles. Each tree has $n$ nodes which are numbered from 1 to $n$.
Dimash has chosen the node $v(1 \leq v \leq n)$, and rooted both trees on that node. After that, he determined the value $\operatorname{sub}_{1}(x)$ - the number of nodes in the subtree of node $x$ in the first tree, and the value $s u b_{2}(x)$ - the number of nodes in the subtree of node $x$ in the second tree. Then he determined the difference of the trees as the number of nodes $x(1 \leq x \leq n)$ such that $\operatorname{sub}_{1}(x)>\operatorname{sub}_{2}(x)$.
Recall that the subtree of a node in a rooted tree is a part of tree consisting of this node and all its descendants. In other words, subtree of a node $x$ is formed by nodes $i$, such that node $x$ is present on the path from the root of the tree to the vertex $i$.
For every node $v(1 \leq v \leq n)$, Dimash wants to find the difference of the trees, if both trees were to be rooted on this node $v$. Help him with this!

## Input

The first line of the input contains one integer $n\left(1 \leq n \leq 5 \cdot 10^{5}\right)$ - the number of nodes in the tree.
Then $n-1$ lines follow, each of them contains two integers $u$ and $v(1 \leq u, v \leq n)$ which describe a pair of nodes connected by an edge in the first tree.
Then $n-1$ lines follow, each of them contains two integers $u$ and $v(1 \leq u, v \leq n)$ which describe a pair of nodes connected by an edge in the second tree.

## Output

Print $n$ space-separated integers, the $i$-th number is the difference of trees, if both trees are rooted on node $i$.

## Scoring

| Subtask | Additional restrictions | Points | Required subtasks |
| :---: | :---: | :---: | :---: |
| 0 | Examples | 0 | - |
| 1 | $n \leq 2000$ | 12 | 0 |
| 2 | $n \leq 100000$ | 22 | 1 |
| 3 | Every node has at most two neighbors | 23 | - |
| 4 | Both trees are complete binary trees | 17 | - |
| 5 | - | 26 | $2,3,4$ |

Recall that complete binary trees are trees where each vertex, except for leaves, has exactly two child vertices, and all leaves are at the same depth.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{ll} \hline 3 & \\ 1 & 2 \\ 2 & 3 \\ 1 & 3 \\ 2 & 3 \end{array}$ | $101$ |
| $\begin{array}{ll} \hline 5 & \\ 1 & 4 \\ 2 & 4 \\ 3 & 2 \\ 3 & 5 \\ 3 & 1 \\ 2 & 3 \\ 5 & 2 \\ 4 & 2 \end{array}$ | 11102 |

## Note

In the first example, when both trees are rooted on node 1 , values of $s u b_{1}$ are $[3,2,1]$ and values of $s u b_{2}$ are $[3,1,2]$. Only for node 2 the condition $s u b_{1}(2)>s u b_{2}(2)$, in other words $2>1$, is satisfied. That is the why answer is 1 .


First tree


Second tree

## Problem C. Golf

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 1 second |
| Memory limit: | 256 megabytes |

Batyr came up with a way to play golf on a directed graph, but a directed gaming graph is required for this.
We refer to a directed graph as a gaming graph if:

1. A graph consists of at least 3 vertices, where the first and second vertices are terminal, and there are no outcoming edges from them.
2. Every vertex has precisely two outgoing edges, except the two terminal ones (both edges can lead to the same vertex).
3. There is a path to at least one of the terminal vertices from each vertex in the graph.

In the beginning, Batyr chooses the starting vertex, different from the terminal vertices, in the directed gaming graph and puts there a ball. Then Batyr starts hitting the ball until it lands in one of the terminal vertices. Since Batyr does not play well, he hits the ball so that it goes through one of the two outgoing edges with equal probability and lands in the vertex this edge leads to.
Construct a directed gaming graph consisting of no more than $n$ vertices, and select a starting vertex in it such that the probability of landing in the terminal vertices is equal to $\frac{a}{a+b}$ for the first terminal vertex and $\frac{b}{a+b}$ for the second.

## Input

Each test contains multiple test cases.
The first line contains two integers $t$ and $n(1 \leq t \leq 100,33 \leq n \leq 100)$ - the number of test cases and the maximum number of vertices for each set.
The first and only line of each test case contains two integers $a$ and $b\left(1 \leq a, b \leq 10^{9}\right)$.

## Output

For each test case, print the graph in the following format.
In the first line two integers $m, s(3 \leq m \leq n, 3 \leq s \leq m)$ - the number of vertices and starting vertex in the graph.
In the each following $m-2$ lines print two integers $v_{i}, u_{i}\left(3 \leq i \leq m, 1 \leq v_{i}, u_{i} \leq m\right)$ - end vertices outgoing from the vertex $i$.
The probability of landing in the vertex 1 starting from vertex $s$ should be $\frac{a}{a+b}$.
The probability of landing in the vertex 2 starting from vertex $s$ should be $\frac{b}{a+b}$.
There should be a path from each vertex to at least one of the terminal vertices.

## Scoring

This task contains 10 subtasks.

XIX Zhautykov Olympiad on Mathematics, Physics and Informatics, *Day 1*
Kazakhstan, Almaty, February, 2, 2023

| Subtask | $n$ | Additional restrictions | Points | Required subtasks |
| :---: | :---: | :---: | :---: | :---: |
| 0 | - | Examples | 0 | - |
| 1 | 100 | $a+b=4$ | 10 | - |
| 2 | 100 | $a+b=32$ | 10 | - |
| 3 | 50 | $a+b=2^{30}$ | 10 | - |
| 4 | 33 | $a, b \leq 15$ | 10 | - |
| 5 | 64 | - | 10 | - |
| 6 | 50 | - | 10 | 5 |
| 7 | 36 | - | 10 | 6 |
| 8 | 35 | - | 10 | 7 |
| 9 | 34 | - | 10 | 8 |
| 10 | 33 | - | 10 | $1,2,3,4,9$ |

## Example

| standard input | standard output |
| :---: | :---: |
| 4100 | 33 |
| 11 | 12 |
| 12 | 43 |
| 13 | 24 |
| 23 | 13 |
|  | 43 |
|  | 42 |
|  | 12 |
|  | 53 |
|  | 45 |
|  | 15 |
|  | 23 |

