

COMMON QUARTERLY EXAMINATION - SEPTEMBER 2019

Standard 10

Reg. No.

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Time Allowed: 2.30 Hours

MATHEMATICS

Maximum Marks: 100

- Instructions:**
1. Check the question paper for fairness of printing. If there is any lack of fairness, inform the Hall Supervisor immediately.
 2. Use Blue (or) Black ink to write and underline and pencil to draw diagrams.

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Note: This question paper contains four parts.

PART - I [MARKS : 14]

Note: i) Answer all the 14 questions.

14×1=14

ii) Choose the most suitable answer from the given four alternatives and write the option code with the corresponding answer.

iii) Each question carries 1 mark.

- 1) $f(x) = (x+1)^3 - (x-1)^3$ represents a function which is
 - a) linear
 - b) cubic
 - c) reciprocal
 - d) quadratic
- 2) If $n(A) = p$ and $n(B) = q$ then $n(A \times B) = \underline{\hspace{2cm}}$.
 - a) $p+q$
 - b) $p-q$
 - c) $p \times q$
 - d) $\frac{p}{q}$
- 3) If $x-6$ is the HCF of $x^2-2x-24$ and x^2-kx-6 then the value of k is
 - a) 3
 - b) 5
 - c) 6
 - d) 8
- 4) $y^2 + \frac{1}{y^2}$ is not equal to
 - a) $\frac{y^4+1}{y^2}$
 - b) $\left(y + \frac{1}{y}\right)^2$
 - c) $\left(y - \frac{1}{y}\right)^2 + 2$
 - d) $\left(y + \frac{1}{y}\right)^2 - 2$
- 5) Product of the roots of the quadratic equation $x^2+3x = 0$ is
 - a) -3
 - b) 3
 - c) 0
 - d) 1
- 6) $7^{4k} \equiv \underline{\hspace{2cm}} \pmod{100}$
 - a) 1
 - b) 2
 - c) 3
 - d) 4
- 7) The next term of the sequence $\frac{3}{16}, \frac{1}{8}, \frac{1}{12}, \frac{1}{18}, \underline{\hspace{2cm}}$ is
 - a) $\frac{1}{24}$
 - b) $\frac{1}{27}$
 - c) $\frac{2}{3}$
 - d) $\frac{1}{81}$
- 8) A sequence is a function defined on the set of $\underline{\hspace{2cm}}$.
 - a) Real numbers
 - b) Natural numbers
 - c) Whole numbers
 - d) Integers

- 9) In $\triangle LMN$, $\angle L = 60^\circ$, $\angle M = 50^\circ$, if $\triangle LMN \sim \triangle PQR$ then the value of $\angle R$ is
 a) 40° b) 70° c) 30° d) 110°
- 10) If in $\triangle ABC$, $DE \parallel BC$, $AB = 3.6$ cm, $AC = 2.4$ cm and $AD = 2.1$ cm then the length of AE is
 a) 1.4 cm b) 1.8 cm c) 1.2 cm d) 1.05 cm
- 11) The area of triangle formed by the points $(-5, 0)$, $(0, -5)$ and $(5, 0)$ is
 a) 0 sq.units b) 25 sq.units c) 5 sq.units d) none of the these
- 12) The inclination of a line whose slope = 1 is
 a) 0° b) 30° c) 45° d) 60°
- 13) $\tan\theta \operatorname{cosec}^2\theta - \tan\theta$ is equal to
 a) $\sec\theta$ b) $\cot^2\theta$ c) $\sin\theta$ d) $\cot\theta$
- 14) The range of the data 8, 8, 8, 8, 8,8 is
 a) 0 b) 1 c) 8 d) 3

PART - II [MARKS : 20]**Answer any TEN questions: [Question No. 28 is compulsory]****10×2=20****Each questions carries 2 marks.**

- 15) If $B \times A = \{(-2, 3), (-2, 4), (0, 3), (0, 4), (3, 3), (3, 4)\}$ find A and B.
- 16) A relation 'f' is defined by $f(x) = x^2 - 2$ where $x \in \{-2, -1, 0, 3\}$.
 (i) List the elements of f. (ii) Is f is a function?
- 17) Find the greatest number that will divide 445 and 572 leaving remainders 4 and 5 respectively.
- 18) Which term of an A.P. 16, 11, 6, 1, is -54?
- 19) Reduce the rational expression $\frac{x^2 - 16}{x^2 + 8x + 16}$ to its lowest form.
- 20) Determine the quadratic equation, whose sum and product of roots are $\frac{-3}{2}$ and -1.
- 21) If $\triangle ABC$ is similar to $\triangle DEF$ such that $BC = 3$ cm, $EF = 4$ cm and area of $\triangle ABC = 54$ cm². Find the area of $\triangle DEF$.
- 22) Prove that $\frac{\cos\theta}{1 + \sin\theta} = \sec\theta - \tan\theta$.
- 23) The standard deviation and mean of a data are 6.5 and 12.5 respectively. Find the co-efficient of variation.
- 24) What is the slope of a line whose inclination is 30° ?

- 25) The line through the points $(-2, a)$ and $(9, 3)$ has slope $-\frac{1}{2}$, find the value of a .
- 26) Let $A = \{1, 2, 3, 4, 5\}$, $B = W$ and $f : A \rightarrow B$ is defined by $f(x) = x^2 - 1$. Find the range of f .
- 27) If a clock strikes once at 1 O'clock, twice at 2 O'clock, thrice at 3 O'clock and so on, how many times will it strike in a day?
- 28) Find the zeros of the quadratic expression $x^2 + 2x - 143$.

PART - III [MARKS : 50]

Answer any TEN questions. Question No. 42 is compulsory.

10×5=50

Each question carries 5 marks.

- 29) Given $A = \{1, 2, 3\}$, $B = \{2, 3, 5\}$, $C = \{3, 4\}$ and $D = \{1, 3, 5\}$, check if $(A \cap C) \times (B \cap D) = (A \times B) \cap (C \times D)$ is true?
- 30) If $f(x) = 3x - 2$, $g(x) = 2x + k$ and if $f \circ g = g \circ f$, then find the value of k .
- 31) The sum of first n , $2n$ and $3n$ terms of an A.P are S_1 , S_2 and S_3 respectively. Prove that $S_3 = 3(S_2 - S_1)$.
- 32) Find the sum of series $6^2 + 7^2 + 8^2 + \dots + 21^2$.
- 33) Find the GCD of the polynomials $3x^4 + 6x^3 - 12x^2 - 24x$, $4x^4 + 14x^3 + 8x^2 - 8x$.
- 34) Find the square root of the expression $\frac{x^2}{y^2} - \frac{10x}{y} + 27 - \frac{10y}{x} + \frac{y^2}{x^2}$.
- 35) State and prove angle bisector theorem.
- 36) If the points $A(-3, 9)$, $B(a, b)$ and $C(4, -5)$ are collinear and if $a + b = 1$ then find a and b .
- 37) Using slope concept, show that the points $(1, -4)$, $(2, -3)$ and $(4, -7)$ form a right angled triangle.
- 38) If $\sin\theta + \cos\theta = p$ and $\sec\theta + \operatorname{cosec}\theta = q$ then prove that $q(p^2 - 1) = 2p$.
- 39) The time taken (in minutes) to complete a homework by 8 students in a day are given by 38, 40, 47, 44, 46, 43, 49, 53. Find the co-efficient of variation.
- 40) The number of books read by 8 students during a month are 2, 5, 8, 11, 14, 6, 12 and 10. Calculate the standard deviation of the data.
- 41) Solve the quadratic equation $5x^2 - 6x - 2 = 0$ by completing the square method.
- 42) If the 4th and 7th term of Geometric Progression are 54 and 1458 respectively, find the Geometric Progression.

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X - Maths

PART - IV [MARKS : 16]**Answer both questions. Each question carries 8 marks.****2×8=16**

- 43) Construct a triangle similar to a given triangle PQR with its sides equal to $\frac{7}{3}$ of the corresponding sides of the triangle PQR.

(OR)

In $\triangle ABC$, if $DE \parallel BC$, $AD = x$, $DB = x-2$, $AE = x+2$ and $EC = x-1$ then find the length of the sides AB and AC.

- 44) Draw the graph of $y = x^2 + 3x - 4$ and hence use it to solve $x^2 + 3x - 4 = 0$.

(OR)

Solve: $\frac{1}{3}(x + y - 5) = y - z = 2x - 11 = 9 - (x + 2z)$.

Quarterly EXAMINATION
 Exam. No. 1010
 Subject Mathematics
 Std. Sec. X-A
 Date 19.09.19

J. Jalye
 19/9/19

page no: 1

M. Fatima

96
 100

V. Good

Total no. of page's written } = 16

Total no. of additional paper } = 6

13
 2
 8
 11
 14
 10
 5
 18
 4
 95+1

part - I

1. d) quadratic.
2. c) $p \times q$
3. c) ~~b~~
4. b) $(y + \frac{1}{y})^2$
5. b) ~~3~~
6. a)
7. b) $\frac{1}{27}$
8. a) real numbers
9. b) 70°
10. a) 1.4 cm
11. b) 25 sq. units.
12. c) 45°
13. d) $\cot \theta$
14. a) \odot

part - II

15) $B \times A = \{(-2, 3), (-2, 4), (0, 3), (0, 4), (3, 3), (3, 4)\}$

$B = \{-2, 0, 3\}$

13

16. $f(x) = x^2 - 2$.

$$x \in \{-2, -1, 0, 3\}$$

Soln:

$$f(x) = x^2 - 2$$

$$\begin{aligned} f(-2) &= (-2)^2 - 2 \\ &= 4 - 2 \\ &= 2. \end{aligned}$$

$$\begin{aligned} f(-1) &= (-1)^2 - 2 \\ &= 1 - 2 \\ &= -1. \end{aligned}$$

$$\begin{aligned} f(0) &= (0)^2 - 2 \\ &= 0 - 2 \\ &= -2. \end{aligned}$$

$$\begin{aligned} f(3) &= (3)^2 - 2 \\ &= 9 - 2 \\ &= 7. \end{aligned}$$

i) $f = \{2, -1, -2, 7\}$

ii)

x	$f(x)$
-2	2
-1	-1
0	-2
3	7

yes, the f is function.

17. the greatest number that divide 445 and 572, remainder = 4 and 5.

Soln:

$$445 - 4 = 441$$

$$572 - 5 = 567$$

using Euclid's division Lemma.

$$44 \overline{) 567} \\ \underline{441} \\ 126$$

Remainder $126 \neq 0$.

again using Euclid's division lemma.

$$126 \overline{) 441} \\ \underline{378} \\ 63$$

Remainder 63 is not equal to zero.

again using Euclid's division lemma.

$$63 \overline{) 126} \\ \underline{126} \\ 0$$

\therefore The greatest number that will divide the 445 and 572 is 63 .

18.

A.P of $16, 11, 6, 1, \dots$ is -54 ?

Soln:

$$t_n = a + (n-1)d$$

$$a = 16$$

$$d = t_2 - t_1$$

$$= 11 - 16$$

$$d = -5$$

$$t_n = -54$$

$$-54 = 16 + (n-1) \cdot -5$$

$$-54 - 16 = -5n + 5$$

$$-70 = -5n + 5$$

$$-70 - 5 = -5n$$

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$$n = \frac{75}{5} = 15$$

$$n = 15$$

19. Reduce : $\frac{x^2 - 16}{x^2 + 8x + 16}$

Soln:

$$\frac{x^2 - 16}{x^2 + 8x + 16}$$

$$= \frac{x^2 - 4^2}{(x+4)(x+4)}$$

$$\begin{array}{c} 16 \\ 4 \times 4 \\ 8 \end{array}$$

$$= \frac{(x+4)(x-4)}{(x+4)(x+4)}$$

$$= \frac{x-4}{x+4}$$

20. Sum of root = $-\frac{3}{2}$

product of root = -1.

Soln:

equation $\Rightarrow x^2 + \underline{\hspace{2cm}}x + \underline{\hspace{2cm}}$

$$x^2 - (\text{sum of root})x + (\text{product of root}) = 0.$$

$$x^2 - \left(-\frac{3}{2}\right)x + (-1) = 0.$$

$$x^2 + \frac{3x}{2} - 1 = 0.$$

$$(x2) \quad 2x^2 + 3x - 2 = 0.$$

$$22. \frac{\cos \theta}{1 + \sin \theta} = \sec \theta - \tan \theta$$

L.H.S \Rightarrow

$$= \frac{\cos \theta}{1 + \sin \theta}$$

$$= \frac{\cos \theta}{1 + \sin \theta} \times \frac{1 - \sin \theta}{1 - \sin \theta}$$

$$= \frac{\cos \theta (1 - \sin \theta)}{1 - \sin^2 \theta}$$

$$= \frac{\cos \theta (1 - \sin \theta)}{\cos^2 \theta}$$

$$= \frac{1 - \sin \theta}{\cos \theta}$$

$$= \frac{1}{\cos \theta} - \frac{\sin \theta}{\cos \theta}$$

$$= \sec \theta - \tan \theta$$

$$= \text{R.H.S.}$$

hence proved.

$$23. \text{C.V} = \frac{\sigma}{\bar{x}} \times 100$$

$$\sigma = 6.5$$

$$\bar{x} = 12.5$$

$$\text{C.V} = \frac{6.5}{12.5} \times 100$$

$$= 0.52$$

$$= 0.52 \times 100$$

$$= 52$$

$$= 52$$

$$\text{C.V} = 52$$

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24. Soln:

$$m = \tan \theta.$$

$$m = \tan 30^\circ$$

$$m = \frac{1}{\sqrt{3}}$$

25.

Soln:points: $(-2, a)$ $(a, 3)$

$$\text{slope: } \frac{y_2 - y_1}{x_2 - x_1}$$

Formula:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$-\frac{1}{2} = \frac{3 - a}{a + 2}$$

$$-\frac{1}{2} = \frac{3 - a}{11}$$

$$-11 = 2(3 - a)$$

$$-11 = 6 - 2a.$$

$$-11 - 6 = -2a.$$

$$+17 = +2a$$

$$a = \frac{17}{2}$$

28.

zeros of polynomial: $p(x) = 0$.

$$x^2 + 2x - 143 = 0.$$

$$(x + 13)(x - 11) = 0.$$

$$x = -13 \text{ or } 11$$

$$\begin{array}{r} -13 \\ 13 \times -11 \\ \hline 2 \end{array}$$

part - III

29) $A = \{1, 2, 3\}$ $B = \{2, 3, 5\}$ $C = \{3, 4\}$ $D = \{1, 3, 5\}$

$$(A \cap C) \times (B \cap D) = (A \times B) \cap (C \times D)$$

$$(A \cap C) \times (B \cap D):$$

$$(A \cap C) = \{3\}$$

$$(B \cap D) = \{3, 5\}$$

$$(A \cap C) \times (B \cap D) = \{3\} \times \{3, 5\}$$

$$= \{(3, 3), (3, 5)\} \quad \text{--- (1)}$$

$$(A \times B) \cap (C \times D):$$

$$A \times B = \{1, 2, 3\} \times \{2, 3, 5\}$$

$$= \{(1, 2), (1, 3), (1, 5), (2, 2), (2, 3), (2, 5), (3, 2), (3, 3), (3, 5)\}$$

$$C \times D = \{3, 4\} \times \{1, 3, 5\}$$

$$= \{(3, 1), (3, 3), (3, 5), (4, 1), (4, 3), (4, 5)\}$$

$$(A \times B) \cap (C \times D) = \{(3, 3), (3, 5)\} \quad \text{--- (2)}$$

from (1) and (2).

$$\text{We get } (A \cap C) \times (B \cap D) = (A \times B) \cap (C \times D).$$

Yes, IFB true.

30) If $f(x) = 3x - 2$, $g(x) = 2x + k$.

$$f \circ g = g \circ f.$$

find k

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$$f \circ g = f(g(x))$$

$$f(2x+k) = 3(2x+k) - 2$$

$$= 6x + 3k - 2 \quad \text{--- (1)}$$

$$g \circ f = g(f(x))$$

$$g(3x-2) = 2(3x-2) + k$$

$$= 6x - 4 + k \quad \text{--- (2)}$$

$$(1) = (2)$$

$$6x + 3k - 2 = 6x - 4 + k$$

$$6x - 6x - 2 + 4 = k - 3k$$

$$2 = -2k$$

$$k = \frac{2}{-2}$$

$$\boxed{k = -1}$$

32. sum of series: $6^2 + 7^2 + 8^2 + \dots + 21^2$

Formula:

$$\frac{n(n+1)(2n+1)}{6}$$

$$= (1^2 + 2^2 + 3^2 + \dots + 21^2) - (1^2 + 2^2 + 3^2 + \dots + 5^2)$$

$$= \left(\frac{21(21+1)(2(21)+1)}{6} \right) - \left(\frac{5(5+1)(2(5)+1)}{6} \right)$$

$$= \left(\frac{21(22)(43)}{6} \right) - \left(\frac{5(6)(11)}{6} \right)$$

$$= \left(\frac{462 \times 43}{6} \right) - \left(\frac{5 \times 66}{6} \right)$$

$$= \left(\frac{3311 \times 43}{4} \right) - \left(\frac{55}{1} \right)$$

$$= 3311 - 55$$

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$$S_n = 3256$$

33. GCD :

$$3x^4 + 6x^3 - 12x^2 - 24x, 4x^4 + 14x^3 + 8x^2 - 8x$$

$$3x^4 + 6x^3 - 12x^2 - 24x$$

$$(\div 3) = x^4 + 2x^3 - 4x^2 - 8x$$

$$x^4 + 2x^3 - 4x^2 - 8x + 0$$

$$\begin{array}{r} 4x \overline{) 4x^4 + 14x^3 + 8x^2 - 8x + 0} \\ \underline{4x^4 + 8x^3 - 16x^2 - 32x + 0} \\ 6x^3 + 24x^2 + 24x \end{array}$$

$$(\div 6) \quad x^3 + 4x^2 + 4x$$

$$x^3 + 4x^2 + 4x$$

$$\begin{array}{r} x - 2 \overline{) x^4 + 2x^3 - 4x^2 - 8x + 0} \\ \underline{x^4 + 4x^3 + 4x^2} \\ -2x^3 - 8x^2 - 8x + 0 \end{array}$$

$$\begin{array}{r} -2x^3 - 8x^2 - 8x + 0 \\ \underline{-2x^3 - 8x^2 - 8x + 0} \\ 0 \end{array}$$

Therefore, the GCD of $[3x^4 + 6x^3 - 12x^2 - 24x, 4x^4 + 14x^3 + 8x^2 - 8x]$ is $x(x^2 + 4x + 4)$.

34. Square root :

$$\frac{x^2}{y^2} - \frac{10x}{y} + 27 - \frac{10y}{x} + \frac{y^2}{x^2}$$

Soln:

$$\frac{x}{y} - 5 + \frac{y}{x}$$

$$\frac{x^2}{y^2} - \frac{10x}{y} + 27 - \frac{10y}{x} + \frac{y^2}{x^2}$$

$$\frac{x^2}{y^2}$$

$$\frac{x^2}{y^2}$$

$$\frac{2x}{y} - 5$$

$$\frac{-10x}{y} + 27$$

$$\frac{-10x}{y} + 25$$

$$\frac{2x}{y} - 10 + \frac{y}{x}$$

$$\frac{-10y}{x} + \frac{y^2}{x^2}$$

$$\frac{-10y}{x} + \frac{y^2}{x^2}$$

0

square root of $\left[\frac{x^2}{y^2} - \frac{10x}{y} + 27 - \frac{10y}{x} + \frac{y^2}{x^2} \right]$ is $\left| \frac{x}{y} - 5 + \frac{y}{x} \right|$

36. A (-3, 9) B(a, b) C (4, -5), a+b=1 — (1) find a and b

Soln:

Area of the triangle : $\frac{1}{2} \{ (x_1y_2 + x_2y_3 + x_3y_1) - (x_2y_1 + x_3y_2 + x_1y_3) \}$ sq. units

$$0 = \frac{1}{2} \begin{vmatrix} -3 & a & 4 & -3 \\ 9 & b & -5 & 9 \end{vmatrix}$$

$$0 = \frac{1}{2} \{ (-3b - 5a + 36) - (9a + 4b + 15) \}$$

$$0 = \frac{1}{2} \{ -3b - 5a + 36 - 9a - 4b - 15 \}$$

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additional sheet no. 4

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$$0 = \frac{1}{2} (-14a - 7b + 21)$$

$$0 = \frac{-14a - 7b + 21}{2}$$

$$-14a - 7b + 21 = 0$$

$$-14a - 7b = -21$$

$$\text{divide by } 7$$

$$-2a - b = -3$$

$$(\div -1)$$

$$2a + b = 3 \quad \text{--- (1)}$$

$$a + b = 1 \quad \text{--- (2)}$$

$$2a + b = 3$$

$$\begin{array}{r} a + b = 1 \\ (-) \quad (-) \quad (-) \\ \hline 2a = 2 \end{array}$$

$$\begin{array}{r} a + b = 1 \\ \quad \quad \quad b = 3 \\ \hline a = 1 \end{array}$$

$$\begin{array}{r} 2a = 2 \\ \quad \quad \quad a = 1 \end{array}$$

$$a = 1 \text{ in eqn (2)}$$

$$1 + b = 1$$

$$b = 1 - 1$$

$$b = 0$$

$$a = 2 \text{ in eqn (2)}$$

$$2 + b = 1$$

$$b = 1 - 2$$

$$b = -1$$

$$a = 2, b = -1$$

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$$38) \sin \theta + \cos \theta = p$$

$$\sec \theta + \operatorname{cosec} \theta = q$$

$$q(p^2 - 1) = 2p.$$

$$p^2 = (\sin \theta + \cos \theta)^2$$

$$= \sin^2 \theta + \cos^2 \theta + 2 \sin \theta \cdot \cos \theta.$$

$$= 1 + 2 \sin \theta \cdot \cos \theta.$$

$$q(p^2 - 1) = 2p$$

$$= \sec \theta + \operatorname{cosec} \theta (1 + 2 \sin \theta \cdot \cos \theta - 1)$$

$$= \frac{1}{\cos \theta} + \frac{1}{\sin \theta} (2 \sin \theta \cdot \cos \theta).$$

$$= \frac{\sin \theta + \cos \theta \times 2 \sin \theta \cdot \cos \theta}{\cos \theta \sin \theta}$$

$$= 2(\sin \theta + \cos \theta).$$

$$= 2p.$$

$$q(p^2 - 1) = 2p$$

hence proved.

$$41) 5x^2 - 6x - 2 = 0.$$

completing square method:

$$\text{soln: } 5x^2 - 6x - 2 = 0.$$

$$(\div 5) \quad 5x^2 - 6x = 2.$$

$$x^2 - \frac{6x}{5} = \frac{2}{5}$$

$$x^2 - \frac{6x}{5} + \left(\frac{6}{5}\right)^2 = \frac{2}{5} + \left(\frac{6}{5}\right)^2$$

$$\left[\frac{(-b)}{(2a)}\right]^2 = \left[\frac{6}{5}\right]^2 = \left(\frac{6}{10}\right)^2$$

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additional sheet no: 5

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~~$$\left(x - \frac{6}{10}\right)^2 = \frac{2}{5} + \frac{36}{100}$$~~

~~$$\left(x - \frac{6}{10}\right)^2 = \frac{20}{100} + \frac{36}{100} = \frac{56}{100} = \frac{14}{25}$$~~

$$\begin{array}{r} 38 \ 19 \\ 4 \ 76 \\ \hline 100 \\ 50 \ 25 \end{array}$$

42. $4^{\text{th}} = 54$ G.P: a, ar, ar^2
 $7^{\text{th}} = 1458$

$$t_n = ar^{n-1}$$

$$t_4 = ar^{4-1}$$

$$54 = ar^3 \quad \text{--- (1)}$$

$$1458 = ar^{7-1}$$

$$1458 = ar^6 \quad \text{--- (2)}$$

$$\frac{ar^3}{ar^6} = \frac{54}{1458} \neq 1$$

$$\frac{1}{r^3} = \frac{1162}{27 \cdot 54}$$

reciprocal. 27.

$$r^3 = 27.$$

$$r = 3$$

$$r = 3 \text{ in eqn (1)}$$

$$ar^3 = 54$$

$$a(3)^3 = 54$$

$$a \times 27 = 54$$

$$a = \frac{54}{27}$$

$$a = 2$$

~~$a = 2$~~

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$$ar = 2 \times 3$$

$$= 6$$

$$ar^2 = 2 \times 3^2$$

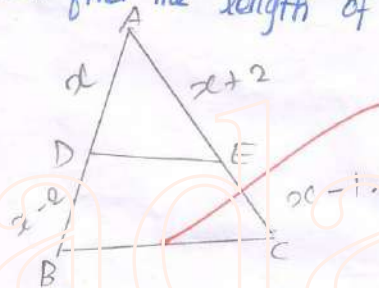
$$= 2 \times 9$$

$$= 18$$

G.P: 2, 6, 18...

part - IV

43. In $\triangle ABC$, if $DE \parallel BC$, $AD = x$, $DB = x - 2$, $AE = x + 2$ and $EC = x - 1$
(or) then find the length of the side AB and AC .

find AB and AC .soln: ~~XXXXXXXXXX~~

By BPT theorem:

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\frac{x}{x-2} = \frac{x+2}{x-1}$$

$$x^2 - x = x^2 - 4$$

$$x^2 - x^2 - x = -4$$

$$-x = -4$$

$$\boxed{x = 4}$$

$$AB = AD + DB$$

$$= x + x - 2$$

$$= 4 + 4 - 2$$

$$\boxed{AB = 6 \text{ cm}}$$

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additional sheet no: 6
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$$\begin{aligned} AC &= AE + EC \\ &= x + 2 + x - 1 \\ &= 2x + 1 \\ &= 2(4) + 1 \\ &= 8 + 1 \\ &= 9 \text{ cm} \end{aligned}$$

$$AC = 9 \text{ cm.}$$

31. soln:

$$S_1 = \frac{n}{2} [2a + (n-1)d]$$

$$S_2 = \frac{2n}{2} [2a + (2n-1)d]$$

$$S_3 = \frac{3n}{2} [2a + (3n-1)d]$$

$$3(S_2 - S_1)$$

$$S_2 - S_1 = \frac{2n}{2} [(2a + (2n-1)d) - \frac{n}{2} [2a + (n-1)d]]$$

$$= \frac{n}{2} [4a + 2(n-1)d] - [2a + (n-1)d]$$

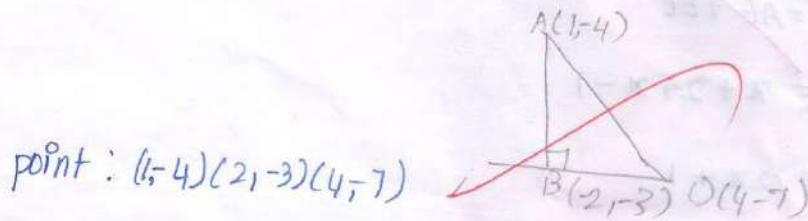
$$S_2 - S_1 = \frac{n}{2} [2a + (3n-1)d]$$

$$3(S_2 - S_1) = \frac{3n}{2} [2a + (3n-1)d]$$

$$3(S_2 - S_1) = S_3$$

hence proved.

37.



$$\text{perpendicular} = m_1 \times m_2 = -1$$

$$\begin{aligned} \text{The slope of AB} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{-3 + 4}{2 - 1} = \frac{1}{1} = 1 \end{aligned}$$

$$\text{The slope of BC} = \frac{-7 + 3}{4 - 2} = \frac{-4}{2} = -2$$

$$\text{The slope of AC} = \frac{-7 + 4}{4 - 1} = \frac{-3}{-3} = 1$$

$$\text{slope of AB} \times \text{slope of AC} = (1)(-1) = -1$$

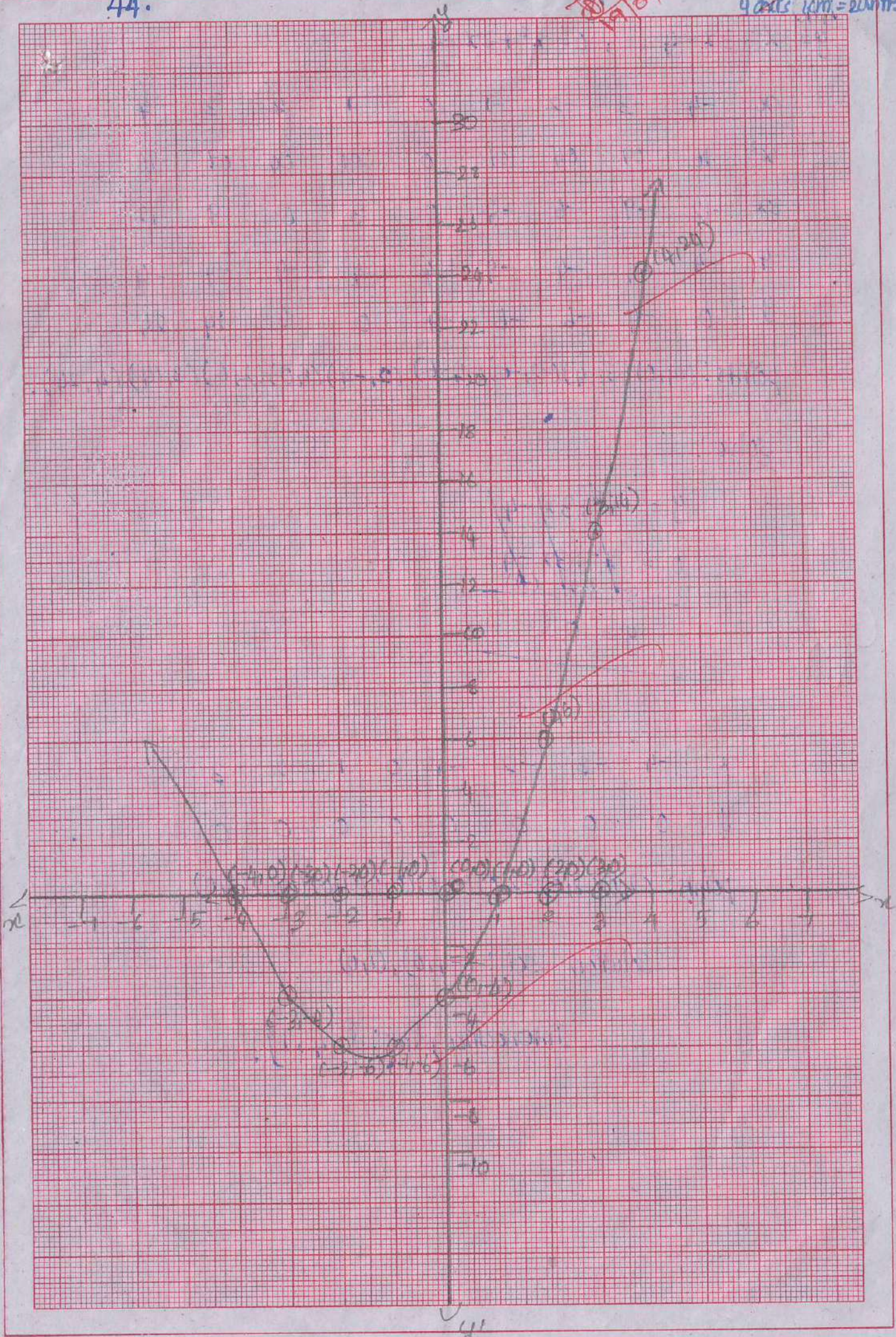
$\triangle ABC$ is a right angled triangle.

hence the proof.

44.

19/10/17

4 cells 1cm = 2 units



part - IV

$y = x^2 + 3x - 4$, $0 = x^2 + 3x - 4$

x	-4	-3	-2	-1	0	1	2	3	4
x ²	16	09	04	01	0	01	04	09	16
3x	-12	-9	-6	-3	0	3	6	9	12
-4	-4	-4	-4	-4	-4	-4	-4	-4	-4
y	0	-4	-6	-6	-4	0	6	14	24

points: (-4,0) (-3,-4) (-2,-6) (-1,-6) (0,-4) (1,0) (2,6) (3,14) (4,24).

solve:

$$y = x^2 + 3x - 4$$

$$0 = x^2 + 3x - 4$$

$$y = 0$$

8

x	-4	-3	-2	-1	0	1	2	3
y	0	0	0	0	0	0	0	0

points: (-4,0) (-3,0) (-2,0) (-1,0) (0,0) (1,0) (2,0) (3,0)

Solution set: (-4,0), (1,0)

Intersecting point: (-4, 1)